Robust Explainable Al: the Case of Counterfactual Explanations

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About me

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Contacts:







Agenda

- Explainable AI
- Counterfactual explanations and recourse
- Robustness
 - what does it mean?
 - why is it needed?
 - **how** can we achieve it?
- Open discussion: robustness and other areas of CS



Explainable AI (XAI)

Techniques and methods that make AI decisions understandable by humans





Explainable AI (XAI)

XAI methods span a wide range of topics within AI and beyond, e.g.

- automated planning
- machine learning (ML)
- human computer interaction



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Today we will focus on explaining deep neural networks (DNNs)

- **high-level** concepts rather than specific algorithms
- fictional use case and explanations



Supervised learning

Training set



Age: 25
Amount: £40K
Duration: 36M

• Amount: £20K

• Duration: 24M

- - accepted

denied

- Age: 82Amount: £26KDuration: 34M

• Age: 32

denied

- Age: 54 • Amount: £
- Amount: £14K
- Duration: 24M
- accepted











Predicted class: denied





Supervised learning

Training set

• Age: 25 denied • Amount: £40K • Duration: 36M • Age: 32 accepted • Amount: £20K • Duration: 24M • Age: 82 • Amount: £26K denied • Duration: 34M

• Age: 54 • Amount: £14K accepted • Duration: 24M

Focus: explaining model predictions



New instance



Predicted class: denied

- Why is it denied?
- Why not accepted?
- How do I get accepted?
- And many more questions...





Challenge



- Age: 30
- Amount: £15K
- Duration: 24M



DNNs are black boxes!

Loan denied



Why is it a problem?











Why is it a problem?

The General Data Protection Regulation (GDPR)

- involved in the decision-making

Art 22: limits to decision-making based solely on automated processing

• Art 13, 2f: right to be provided with meaningful information about the logic



How to achieve XAI?

Interpretable models

- Linear models
- Decision trees
- Rule-based models





- Deep networks
- Ensemble models



How to achieve XAI?

Interpretable models

- Linear models
- Decision trees
- Rule-based models







Counterfactual explanations (CXs)

Original instance



Loan denied





Counterfactual explanations (CXs)

Original instance



Loan denied



Counterfactual explanation



The application would have been accepted had you asked for £10K instead of £15K





Consider the neural network \mathcal{M} below:









Consider the neural network \mathcal{M} below:



• Given input $x_F = [1,2], M$ predicts class 1 ($y_1 > y_0$)







Consider the neural network *M* below:



- Given input $x_F = [1,2]$, \mathcal{M} predicts class 1 ($y_1 > y_0$)



• A possible CX may be x = [2.1,2], for which \mathcal{M} predicts class 0



- Given an input x_F and a binary classifier \mathcal{M} such that $\mathcal{M}(x_F) = c$
- A distance function d



- Given an input x_F and a binary classifier \mathcal{M} such that $\mathcal{M}(x_F) = c$
- A distance function d
- A counterfactual explanation x is computed as:
 - $\arg\min d(x_F, x)$ $\boldsymbol{\chi}$

subject to $\mathcal{M}(x) = 1 - c$



Most approaches solve relaxation defined as:

$\underset{x}{\operatorname{arg\,min}} \ell(\mathscr{M}(x), 1 - c) + \lambda \cdot d(x_F, x)$

Counterfactual explanations without opening the black box: automated decisions and the GDPR. Wachter et al, Harvard Journal of Law & Technology 2018.



Most approaches solve relaxation defined as:



where:

• ℓ is a differentiable loss function which minimises the gap between current and desired prediction

Counterfactual explanations without opening the black box: automated decisions and the GDPR. Wachter et al, Harvard Journal of Law & Technology 2018.

$$1-c) + \lambda \cdot d(x_F, x)$$



Most approaches solve relaxation defined as:

 $\arg\min\,\ell(\mathcal{M}(x),$ $\boldsymbol{\chi}$

where:

- ℓ is a differentiable loss function which minimises the gap between current and desired prediction
- λ controls distance trade-off

Counterfactual explanations without opening the black box: automated decisions and the GDPR. Wachter et al, Harvard Journal of Law & Technology 2018.

$$1-c)+\lambda\cdot d(x_F,x)$$



Tool support

AI Explainability 360 (v0.3.0)

Build passing docs passing pypi package 0.2.1

The AI Explainability 360 toolkit is an open-source library that supports interpretability and explainability of datasets and machine learning models. The AI Explainability 360 Python package includes a comprehensive set of algorithms that cover different dimensions of explanations along with proxy explainability metrics. The AI Explainability 360 toolkit supports tabular, text, images, and time series data.

The AI Explainability 360 interactive experience provides a gentle introduction to the concepts and capabilities by walking through an example use case for different consumer personas. The tutorials and example notebooks offer a deeper, data scientist-oriented introduction. The complete API is also available.

There is no single approach to explainability that works best. There are many ways to explain: data vs. model, directly interpretable vs. post hoc explanation, local vs. global, etc. It may therefore be confusing to figure out which algorithms are most appropriate for a given use case. To help, we have created some guidance material and a taxonomy tree that can be consulted.

https://github.com/Trusted-AI/AIX360

C license BSD-3-Clause pytorch v0.6.0 pypi v0.6.0 circleci failing platform noarch conda-forge v0.6.0	
Captum is a model interpretability and understanding library for PyTorch. Captum means comprehension in and contains general purpose implementations of integrated gradients, saliency maps, smoothgrad, vargra others for PyTorch models. It has quick integration for models built with domain-specific libraries such as torchvision, torchtext, and others.	ı Latin ıd and

Captum is currently in beta and under active development!

https://github.com/pytorch/captum



Alibi is an open source Python library aimed at machine learning model inspection and interpretation. The focus of the library is to provide high-quality implementations of black-box, white-box, local and global explanation methods for classification and regression models.

https://github.com/SeldonIO/alibi

CARLA - Counterfactual And Recourse Library

CARLA is a python library to benchmark counterfactual explanation and recourse models. It comes out-of-the box with commonly used datasets and various machine learning models. Designed with extensibility in mind: Easily include your own counterfactual methods, new machine learning models or other datasets. Find extensive documentation here! Our arXiv paper can be found here.



What is algorithmic recourse? As machine learning (ML) models are increasingly being deployed in high-stakes applications, there has been

growing interest in providing recourse to individuals adversely impacted by model predictions (e.g., below we depict the canonical recourse example for an applicant whose loan has been denied). This library provides a starting point for researchers and practitioners alike, who wish to understand the inner workings of various counterfactual explanation and recourse methods and their underlying assumptions that went into the design of these methods.

https://github.com/carla-recourse/CARLA



Is minimising distance always good?



CXs are often indistinguishable from adversarial examples!

Exploring Counterfactual Explanations Through the Lens of Adversarial Examples: A Theoretical and Empirical Analysis. Pawelczyk et al, AISTATS 2022.



Brittle explanations ahead!



Threats

- 1. Input perturbations
- 2. Model perturbations
- 3. Model multiplicity
- 4. Noisy execution



Robust XA



List of references is partial - too much to cover in 90 minutes!

Threats

- 1. Input perturbations
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Robust XA



Threats

- Input perturbations 1.
- 2. Model perturbations
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Heuristic vs Exhaustive robustness guarantees



Brittle explanations ahead!



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Age: 30
Amount: £15K
Duration: 24M
Age: 30
Age: 30
Amount: £13K
Duration: 24M





•Age: 30

- •Amount: £15K
- Duration: 24M

X

 \bigotimes

Age: 30
Amount: £13K
Duration: 24M

• Duration: 24M

•Age: 30

- •Amount: £16K
- Duration: 24M





•Age: 30

- •Amount: £15K
- Duration: 24M

X

 \bigotimes

0

Age: 30
Amount: £13K
Duration: 24M

- Duration: 24M
- •Age: 30
- •Amount: £16K
- Duration: 24M
- •Age: 30
- •Amount: £10K
- Duration: 12M


Lack of robustness to input changes poses a number of problems!

we expect phenomena in the world that are similar to have similar explanations

Robustness in Machine Learning Explanations: Does it Matter? Hancox-Li, FAT* 2020.





Lack of robustness to input changes poses a number of problems!

we expect phenomena in the world that are similar to have similar explanations

- is the explanation really capturing how the black-box works?

Robustness in Machine Learning Explanations: Does it Matter? Hancox-Li, FAT* 2020.

we would expect neighbouring inputs to be processed in similar ways

uncertainty in how data is collected may have huge impact on explanation







Counterfactual Explanations Can Be Manipulated. Slack et al, NeurIPS 2021.

Can be exploited to train adversarial models that generate unfair explanations!



(b) **Training Adversarial Model**





Input perturbations may invalidate CXs!

 \bullet



On the Adversarial Robustness of Causal Algorithmic Recourse. Dominguez-Olmedo et al, ICML 2022.

Dominguez-Olmedo propose a method to preserve validity (minmax formulation)





Zhang et al propose to use **density** to guide CX search

• Similar inputs should "gravitate" towards similar CXs



Density-based Realiable and Robust Explainer for Counterfactual Explanations. Zhang et al, Expert Systems with Applications, 2023.







Brittle explanations ahead!



Threats

1. Input perturbations

2. Model perturbations

- 3. Model multiplicity
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to







to









t1

t₀









t1

to











 t_1

to













t1

t₀







tn+1









t1

t₀







tn+1









t1

to













Model shifts may occur as a result of data shifts



Model shifts may occur as a result of data shifts

Dilemma







Model shifts may occur as a result of data shifts

Dilemma

• **Trust** the old CX, although possibly contradicted by new data





Model shifts may occur as a result of data shifts

Dilemma

- Trust the old CX, although possibly contradicted by new data
- Trash the old CX, possibly upsetting end users





Ferrario and Loi proposed an augmentation technique to mitigate the issue







Ferrario and Loi proposed an augmentation technique to mitigate the issue







Ferrario and Loi proposed an augmentation technique to mitigate the issue

τn





Ferrario and Loi proposed an augmentation technique to mitigate the issue

τn





Ferrario and Loi proposed an augmentation technique to mitigate the issue











Upadhyay et al use a minmax formulation to inject model robustness

Towards Robust and Reliable Algorithmic Recourse. Upadhyay et al, NeurIPS, 2021.



Upadhyay et al use a minmax formulation to inject model robustness

• Assume the existence of a set of plausible model shifts Δ



Upadhyay et al use a minmax formulation to inject model robustness

- Assume the existence of a set of plausible model shifts Δ
- Use \mathscr{M}_{δ} to denote perturbed version of \mathscr{M} under $\delta \in \Delta$

$\arg\min \arg\max \ell(\mathscr{M}_{\delta}(x), 1-c) + \lambda \cdot d(x_F, x)$ $\delta \in \Delta$ $\boldsymbol{\chi}$

Towards Robust and Reliable Algorithmic Recourse. Upadhyay et al, NeurIPS, 2021.



Upadhyay et al use a minmax formulation to inject model robustness

- Assume the existence of a set of plausible model shifts Δ
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Towards Robust and Reliable Algorithmic Recourse. Upadhyay et al, NeurIPS, 2021.



Jiang et al use interval abstractions to obtain formal robustness guarantees



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Jiang et al use interval abstractions to obtain formal robustness guarantees







Brittle explanations ahead!



Threats

- 1. Input perturbations
- 2. Model perturbations
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Model multiplicity

Situation where models of equal accuracy differ in the process by which they reach a given prediction





Model Multiplicity: Opportunities, Concerns, and Solutions. Black et al, ACM FAccT'22.







Model multiplicity



- Age: 30
- Amount: £15K
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Model multiplicity



- Age: 30
- Amount: £15K
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Model multiplicity



- Age: 30
- Amount: £10K
 Duration: 24M



Model multiplicity



- Age: 30
- Amount: £10K
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Model multiplicity



- Age: 30
- Amount: £10K
- Duration: 24M









Implications

- Different models might offer better/worse recourse options



Increase by £50



That's not enough!

Disagreeing models might raise concerns about the justifiability of CXs

Erm, I'll leave you alone now...



Black et al present an extensive discussion on model multiplicity

Not targeting CXs specifically but also applicable to XAI



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Not targeting CXs specifically but also applicable to XAI

They propose some approaches to deal with multiplicity:

Model Multiplicity: Opportunities, Concerns, and Solutions. Black et al, ACM FAccT'22.



Black et al present an extensive discussion on model multiplicity

Not targeting CXs specifically but also applicable to XAI

They propose some approaches to deal with multiplicity:

Meta-rules





"Always choose the model that has at least 95% accuracy"









Black et al present an extensive discussion on model multiplicity

Not targeting CXs specifically but also applicable to XAI

They propose some approaches to deal with multiplicity:

Meta-rules

Majority voting

Model Multiplicity: Opportunities, Concerns, and Solutions. Black et al, ACM FAccT'22.



"Two out of three agree, they must be correct"









Black et al present an extensive discussion on model multiplicity

Not targeting CXs specifically but also applicable to XAI

They propose some approaches to deal with multiplicity:

- Meta-rules
- Majority voting
- **Randomised choice**

Model Multiplicity: Opportunities, Concerns, and Solutions. Black et al, ACM FAccT'22.



"Sample a model and use it"









Pawelczyk et al analyse robustness of CXs under model multiplicity:

On Counterfactual Explanations under Predictive Multiplicity. Pawelczyk et al, UAI 2020.







Pawelczyk et al analyse robustness of CXs under model multiplicity:

• CXs on data manifold are more robust

On Counterfactual Explanations under Predictive Multiplicity. Pawelczyk et al, UAI 2020.





Pawelczyk et al analyse robustness of CXs under model multiplicity:

- CXs on data manifold are more robust
- Robust CXs are more expensive

On Counterfactual Explanations under Predictive Multiplicity. Pawelczyk et al, UAI 2020.





Leofante et al present an approach to generate robust CXs under multiplicity

Counterfactual Explanations and Model Multiplicity: a Relational Verification View. Leofante et al, KR 2023.



Leofante et al present an approach to generate robust CXs under multiplicity

Assumes pre-defined set of models





Counterfactual Explanations and Model Multiplicity: a Relational Verification View. Leofante et al, KR 2023.





- Assumes pre-defined set of models
- Builds product network to reason under multiplicity in one go



Counterfactual Explanations and Model Multiplicity: a Relational Verification View. Leofante et al, KR 2023.

Leofante et al present an approach to generate robust CXs under multiplicity

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Brittle explanations ahead!



Threats

- 1. Input perturbations
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Age: 30 Amount: £15K Duration: 24M





Age: 30 Amount: £15K Duration: 24M • Age: 30 Age: 30 Amount: £10K Duration: 24M









- •Ag •An •Du
 - •Age: 30
 - •Amount: £9.9K
 - •Duration: 24M









• Duration: 24M



Implications

Recourses are often noisily implemented in real-world settings

- Noise may **invalidate** CX
- Jeopardise explanatory function
- **Reduce** trust

Manipulation-Proof Machine Learning. Björkegren et al, arxiv preprint https://arxiv.org/abs/2004.03865, 2020.







Probabilistically Robust Recourse: Navigating the Trade-offs between Costs and Robustness in Algorithmic Recourse. Pawelczyk et al, ICLR 2023.



• Given input x_F , CX x and model \mathcal{M}





- Given input x_F , CX x and model \mathcal{M}
- Define invalidation rate $\Delta(x) = \mathbb{E}_{\epsilon}[\mathcal{M}(x) \mathcal{M}(x + \epsilon)]$

Probabilistically Robust Recourse: Navigating the Trade-offs between Costs and Robustness in Algorithmic Recourse. Pawelczyk et al, ICLR 2023.



- Given input x_F , CX x and model \mathcal{M}
- Define invalidation rate $\Delta(x) = \mathbb{E}_{\epsilon}[\mathcal{M}(x) \mathcal{M}(x + \epsilon)]$
- Define noise-aware loss \mathscr{L} as

$$\lambda_1 \cdot \ell_1(\Delta(x), \rho) + \lambda_2 \cdot \ell$$

Probabilistically Robust Recourse: Navigating the Trade-offs between Costs and Robustness in Algorithmic Recourse. Pawelczyk et al, ICLR 2023.

 $\mathcal{P}_2(\mathcal{M}(x), 1-c) + \lambda_3 \cdot d(x_F, x))$



- Given input x_F , CX x and model \mathcal{M}
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 $\mathcal{P}_2(\mathcal{M}(x), 1-c) + \lambda_3 \cdot d(x_F, x))$



Leofante and Lomuscio use formal verification to identify robust CXs



Leofante and Lomuscio use formal verification to identify robust CXs

• Given a CX x and model \mathcal{M}





Leofante and Lomuscio use formal verification to identify robust CXs

- Given a CX x and model \mathcal{M}
- Check local robustness of *M* around *x* using verifiers





Leofante and Lomuscio use formal verification to identify robust CXs

- Given a CX x and model \mathcal{M}
- Check local robustness of *M* around *x* using verifiers





Leofante and Lomuscio use formal verification to identify robust CXs

- Given a CX x and model .///
- Check local robustness of *M* around *x* using verifiers
- CX guaranteed to be robust when safe radius identified





Summing up

- CX generation methods focus on minimising distance
- This may result in brittle explanations
- We have examined lack of robustness in four scenarios:
 - input noise, model shifts, model multiplicity and noisy execution
- Can we borrow ideas from other areas of CS to fix this?



Some interesting (relevant) directions

Robustness and...

- Formal Explainable AI
- Fairness in ML
- Formal verification of neural networks
- Privacy
- Others?

Delivering Trustworthy AI through Formal XAI. Marques-Silva and Ignatiev, AAAI 2022. Counterfactual Explanations Can Be Manipulated. Slack et al, NeurIPS 2021. Algorithms for Verifying Deep Neural Networks. Liu et al, Found. Trends Optim. 4(3-4): 244-404, 2021. On the Privacy Risks of Algorithmic Recourse. Pawelczyk et al, AISTATS 2023.



Thank you!

Contacts:





References

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- Towards Robust Contrastive Explanations for Human-Neural Multi-agent Systems. Leofante and Lomuscio, AAMAS 2023.
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